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$$9.) f'(x) = (2 \cos(3x + 1)) \cdot 3 = 6 \cos(3x + 1)$$

$$22.) f'(x) = -5(-\sin(2 - x^3))(-3x^2) = -15x^2 \sin(2 - x^3)$$

$$\begin{aligned} 38.) f'(x) &= \tan x \left(\frac{d}{dx} \cot x \right) + \left(\frac{d}{dx} \tan x \right) \cot x = \tan x (-\csc^2 x) + (\sec^2 x) \cot x \\ &= \frac{\sin x}{\cos x} \left(-\frac{1}{\sin^2 x} \right) + \left(\frac{1}{\cos^2 x} \right) \frac{\cos x}{\sin x} \\ &= -\frac{1}{\cos x \sin x} + \frac{1}{\cos x \sin x} \\ &= 0 \end{aligned}$$

Alternatively, one could say that

$$f(x) = \tan x \cot x = \tan x \left(\frac{1}{\tan x} \right) = 1$$

So

$$f'(x) = \frac{d}{dx} 1 = 0$$

$$\begin{aligned} 32.) g'(t) &= \frac{\cos(5t) \left(\frac{d}{dt} \sin(3t) \right) - \sin(3t) \left(\frac{d}{dt} \cos(5t) \right)}{\cos^2(5t)} \\ &= \frac{\cos(5t)(3 \cos(3t)) - \sin(3t)(-5 \sin(5t))}{\cos^2(5t)} \\ &= \frac{3 \cos(5t) \cos(3t) + 5 \sin(3t) \sin(5t)}{\cos^2(5t)} \end{aligned}$$

59.) A horizontal tangent has slope zero. So we find when $y' = 0$.

$$y' = (\cos(\frac{\pi}{3}x))(\frac{\pi}{3}) = 0$$

Dividing both sides by $\frac{\pi}{3}$:

$$\cos(\frac{\pi}{3}x) = 0$$

So

$$\frac{\pi}{3}x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}, \dots$$

Multiplying both sides by $\frac{3}{\pi}$ gives

$$x = \frac{3}{2}, \frac{9}{2}, \frac{15}{2}, \frac{21}{2}, \dots$$

which is to say

$$x = \frac{3+6k}{2}$$

for any integer k . Next, we find the y -coordinate for the x 's we found:

$$y = \sin\left(\frac{\pi}{3} \frac{3+6k}{2}\right) = \sin\left(\pi \frac{1+2k}{2}\right)$$

$$\begin{aligned}
&= \begin{cases} \sin(\frac{\pi}{2}) & \text{if } k \text{ is even} \\ \sin(\frac{3\pi}{2}) & \text{if } k \text{ is odd} \end{cases} \\
&= \begin{cases} 1 & \text{if } k \text{ is even} \\ -1 & \text{if } k \text{ is odd} \end{cases}
\end{aligned}$$

So the points are

$$(x, y) = \begin{cases} (\frac{3+6k}{2}, 1) & \text{if } k \text{ is even} \\ (\frac{3+6k}{2}, -1) & \text{if } k \text{ is odd} \end{cases}$$

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$$\begin{aligned}
1.) \quad f(x) &= -3x^4 + 2x^{-\frac{1}{2}} + 1 \\
f'(x) &= -3(4x^3) + 2(-\frac{1}{2})x^{-\frac{3}{2}} = -3x^4 - x^{-\frac{3}{2}}
\end{aligned}$$

$$\begin{aligned}
2.) \quad g(x) &= (x^3 + 4)^{-\frac{1}{2}} \\
g'(x) &= (-\frac{1}{2})(x^3 + 4)^{-\frac{3}{2}}(3x^2) = -\frac{3}{2}(x^3 + 4)^{-\frac{3}{2}}
\end{aligned}$$

$$\begin{aligned}
6.) \quad g'(s) &= \frac{\cos(3x)(\frac{d}{ds} \sin(3s+1)) - \sin(3s+1)(\frac{d}{ds} \cos(3s))}{\cos^2(3s)} \\
&= \frac{\cos(3x)((\cos(3s+1))(3)) - \sin(3s+1)((-\sin(3s))(3))}{\cos^2(3s)} \\
&= \frac{3 \cos(3x) \cos(3s+1) + 3 \sin(3s+1) \sin(3s)}{\cos^2(3s)}
\end{aligned}$$

$$\begin{aligned}
10.) \quad g(x) &= \tan(x^2 + 1) \\
g'(x) &= (\sec^2(x^2 + 1))(2x) = 2x \sec^2(x^2 + 1) \\
g''(x) &= 2x(\frac{d}{dx} \sec^2(x^2 + 1)) + (\frac{d}{dx} 2x) \sec^2(x^2 + 1) \\
&= 2x(2 \sec(x^2 + 1) \sec(x^2 + 1) \tan(x^2 + 1) 2x) + (2) \sec^2(x^2 + 1) \\
&= 8x^2 \sec(x^2 + 1) \sec(x^2 + 1) \tan(x^2 + 1) + 2 \sec^2(x^2 + 1)
\end{aligned}$$

$$\begin{aligned}
31.) \quad p(x) &= ax^2 + bx + c \\
p'(x) &= 2ax + b \\
p''(x) &= 2a
\end{aligned}$$

Going from last line to first

$$p''(0) = 2a = 4 \text{ means } a = 2$$

So

$$p'(x) = 2(2)x + b = 4x + b$$

Then

$$p'(1) = 4(1) + b = 8 \text{ means } b = 4$$

So

$$p(x) = 2x^2 + 4x + c$$

Finally

$$\begin{aligned} p(-1) &= 2(-1)^2 + 4(-1) + c = 6 \\ 2 - 4 + c &= 6 \\ c &= 8 \end{aligned}$$

Thus

$$p(x) = 2x^2 + 4x + 8$$