Math 104

Homework 4

Due Wednesday, October 28, 2009

- 1. Exercise 3.5, Chapter 3 of Trefethen-Bau.
- 2. Let U be an $m \times m$ arbitrary unitary matrix. Show that $||UA||_2 = ||A||_2$ and that $||UA||_F = ||A||_F$. Deduce from this that we also have $||AV||_2 = ||A||_2$ and $||AV||_F = ||A||_F$, where V is an $n \times n$ (arbitrary) unitary matrix.
- 3. Exercise 5.3, Chapter 5 of Trefethen-Bau.
- 4. Exercise 6.1, Chapter 6 of Trefethen-Bau.
- 5. Consider the square matrices A and $B = A + \mu I$ for some scalar $\mu \in \mathbb{C}$. How do the eigenvalues and eigenvectors of B relate to those of A?