## Homework 4

Due Wednesday, October 28, 2009

1. Exercise 3.5, Chapter 3 of Trefethen-Bau.
2. Let $U$ be an $m \times m$ arbitrary unitary matrix. Show that $\|U A\|_{2}=\|A\|_{2}$ and that $\|U A\|_{F}=\|A\|_{F}$. Deduce from this that we also have $\|A V\|_{2}=\|A\|_{2}$ and $\|A V\|_{F}=\|A\|_{F}$, where $V$ is an $n \times n$ (arbitrary) unitary matrix.
3. Exercise 5.3, Chapter 5 of Trefethen-Bau.
4. Exercise 6.1, Chapter 6 of Trefethen-Bau.
5. Consider the square matrices $A$ and $B=A+\mu I$ for some scalar $\mu \in \mathbb{C}$. How do the eigenvalues and eigenvectors of $B$ relate to those of $A$ ?
