Meeting: 1003, Atlanta, Georgia, SS 10A, AMS Special Session on Dynamics of Mapping Class Groups on Moduli Spaces, I

1003-57-680 Joseph P Previte* (jpp4@psu.edu), Penn State Erie, School of Science, Station Road, Erie, PA 16563, and Eugene Z Xia. Dynamics of the mapping class group on the moduli of a punctured sphere with rational holonomy.

Let M be a four-holed sphere and Γ the mapping class group of M fixing the boundary ∂M . The group Γ acts on $M_B(SL(2,C)) = Hom_B^+(\pi_1(M), SL(2,C))/SL(2,C)$ which is the space of completely reducible SL(2,C)-gauge equivalence classes of flat SL(2,C)-connections on M with fixed holonomy B on ∂M . Let $B \in (-2,2)^4$ and M_B be the compact component of the real points of $M_B(SL(2,C))$. These points correspond to SU(2)-representations or SL(2,R)-representations. The Γ -action preserves M_B and we study the topological dynamics of the Γ -action on M_B and show that for a dense set of holonomy $B \in (-2,2)^4$, the Γ -orbits are dense in M_B . We also produce a class of representations $\rho \in Hom_B^+(\pi_1(M), SL(2,R))$ such that the Γ -orbit of $[\rho]$ is finite in the compact component of $M_B(SL(2,R))$, but $\rho(\pi_1(M))$ is dense in SL(2,R). (Received September 27, 2004)