

Lecture Questions I: 110.302 Differential Equations

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Question 1

Determine the truth of the following two statements:

- ① Every separable ODE can be written as an exact ODE.
 - ② Every linear ODE can be written as a separable ODE.
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- A. Both are true.
 - B. (1) is true and (2) is false.
 - C. (1) is false and (2) is true.
 - D. Both are false.

Question 2: Let $\dot{x} = x^2 - 2x + c$, for $c \in \mathbb{R}$.

For $c = -15$, the phase line for the ODE has the following characteristics:

- A. A sink at $x = -3$ and a source at $x = 5$.
- B. A source at $x = -3$ and a sink at $x = 5$.
- C. A sink at $x = -5$ and a source at $x = 3$.
- D. A source at $x = -5$ and a sink at $x = 3$.
- E. Not enough information to tell.

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- D. A source at $x = -5$ and a sink at $x = 3$.
- E. Not enough information to tell.

For $c = -15$ and $x(0) = 0$, $\lim_{t \rightarrow -\infty} x(t) =$

- A. $-\infty$.
- B. ∞ .
- C. The sink in your previous answer.
- D. The source in your previous answer.
- E. None of the above.

Question 3

The ODE

$$\left(\sin t + \sqrt{2-t}\right) y + e^{t \ln(t+1)} \left(t^2 - 10^{-2000}\right) y' = t^4$$

is linear. By the Existence and Uniqueness Theorem for first-order linear ODEs, we know the following:

- A. Solutions are not guaranteed to exist at all at the point $(0, 2) \in \mathbb{R}^2$.
- B. Solutions are guaranteed to exist but may not be unique at $(0, 2)$.
- C. A solution exists and is unique passing through $(0, 2)$.
- D. There is not enough information to determine whether solutions exist and/or are unique at $(0, 2)$.
- E. I have no idea.