| problem | 1 | 2 | 3 | 4 | 5 | 6 | 7 | total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| scores |  |  |  |  |  |  |  |  |

Exam \#2, October 26, Calculus II (109), Fall, 2011, W. Stephen Wilson

I agree to complete this exam without unauthorized assistance from any person, materials or device.

Name (signature): $\qquad$ Date: $\qquad$

Name (print): $\qquad$

TA Name and section: $\qquad$

NO CALCULATORS, NO PAPERS, NOT MUCH PARTIAL CREDIT, SHOW WORK. (30 points total)

In case you need them: $\cos (2 x)=2 \cos ^{2}(x)-1=1-2 \sin ^{2}(x)$.

All solutions must be placed in the box provided.

There is an extra page to show work on for each problem.

1. (4 points total) Let $r=4 \cos (\theta)+2 \sin (\theta)$.

Find the maximum $r$. (1 point)


Find an associated $\theta$. (1 point)


Find the Cartesian coordinates (i.e. $(x, y))$ for this point. (2 points, 1 each coordinate)


Space for problem \# 1.
2. (4 points total) Let $r=4 \cos (\theta)+2 \sin (\theta)$.

Find the $x$ values for the two points the graph crosses the $x$-axis. (2 points, 1 each)


Find the $y$ values for the two points the graph crosses the $y$-axis. (2 points, 1 each)


Space for problem \# 2 .
3. (4 points total) Let $r=4 \cos (\theta)+2 \sin (\theta)$.

This can be a long tedius calculation, easy to make mistakes on. I recommend this for last.
Find the slope of the tangent line to the curve at each of the two points that the curve intersects the $x$-axis. ( 2 points, 1 point each) Be sure to specify which point goes with which slope. ( 2 points, 1 point each)


Space for problem \# 3 .
4. (4 points total) Let $r=4 \cos (\theta)+2 \sin (\theta)$.

Set up the integral for the area enclosed by the curve, the $x$-axis, and the $y$-axis when $0 \leq x$ and $0 \leq y$, (i.e. the first quadrant). ( 2 points for correct answer, 1 for something close)


Evaluate the integral to find this area. (2 points for correct answer, 1 point for something close)


Space for problem \# 4.
5. (4 points total) Let $r=4 \cos (\theta)+2 \sin (\theta)$.

Set up the integral for the length of the curve in the first quadrant, i.e. when $0 \leq x$ and $0 \leq y$. (2 points for correct answer, 1 point for something close)


Evaluate the integral to find this length. (2 points for correct answer, 1 point for something close)
$\square$

Space for problem \# 5 .
6. (4 points total) Let $x=\sin (t)$ and $y=t^{3}-3 t$.

Find the $x$ and $y$ coordinates for the two points that $\frac{d y}{d x}=0$. (2 points each, 1 for each coordinate)


Space for problem \# 6 .
7. (6 points total) Compute $\frac{d^{2} y}{d x^{2}}$ in terms of $t$. (2 points for correct answer, 1 for something close)


There are two local max/min. For each one, identify the point, the value of the second derivative, $\frac{d^{2} y}{d x^{2}}$, and state if it is the local maximum or the local minimum. (2 points each)


Space for problem \# 7 .

