Math773 **Topics Topics in Data Science**

Part I: Learning kernels in operators

Part II: Probability theory for TSC

Part III: Time series modeling

Fei Lu, Fall 2023

Part I: Learning kernels in operators

- **Overview and review of nonparametric regression**
- **Finitely many particles**
- Coercivity
- Infinitely many particles: mean-field
- **DARTR** and its Bayesian perspective
- **Small noise analysis**

References:

- CS02: Felipe Cucker and Steve Smale. On the mathematical foundations of learning. Bulletin of the American mathematical society, 39(1):1–49, 2002.

- GKKH02: Laszlo Gyorfi, Michael Kohler, Adam Krzyzak, and Harro Walk. A distribution-free theory of nonparametric regression. Springer, 2002.

- Tsy08: AB Tsybakov. Introduction to nonparametric estimation. Springer 2008. - Maggioni etc.

Week 1-6, lectures

Part II: Probability theory for TSC

- Time Series Classification methods
- + Random Forest: Mur22intro, Chp18
- + ROCKET
- + ResNet
- + Signature methods

- Theory: Bayes error

+ DGL96: Luc Devroye, Laszlo Gyorfi, and Gabor Lugosi. A probabilistic theory of pattern recognition, volume 31. Springer Science & Business Media, 1996. chp2,6,7,8,12

+ Mur22intro: Kevin P Murphy. Probabilistic machine learning: an introduction. MIT press, 2022. + Mur22adv: Kevin P Murphy. Probabilistic machine learning: advanced topics. MIT press, 2022.

Week 7-10: presentations+lectures

Part III: Time series modeling

- Neural Network for Sequences

Mur22intro: Part III, Deep Neural Networks

- + chp13: Neural Networks
- + chp14: Neural Networks for images
- + chp15: Neural Networks for sequences

Mur22adv: Part III Prediction

- + chp14: predictive models: an overview
- + chp15: Generalized linear models
- + chp16: Deep Neural Networks
- + chp17: Bayesian Neural networks
- + chp18: Gaussian processes

Week 11-15: presentations+lectures