

Math 631: Problem Set 3 due in class Monday, March 21

1. Evans p.86: 10
2. Evans p.88: 18
3. Evans p.88: 19
4. Evans p.88: 24
5. Solve $u_{tt} - u_{xx} = 0$ on $(0, L) \times (0, \infty)$
 $u = g, u_t = 0$ on $(0, L) \times \{t = 0\}$ $u = 0$ on $(\{0\} \cup \{L\}) \times (0, \infty)$.

by converting to a problem on $R \times (0, \infty)$ using odd reflection.

Conclude that

$$u(x, t) = \frac{1}{2} \left\{ \sum B_n \sin\left(\frac{n}{\pi}(x+t)\right) + \sum B_n \sin\left(\frac{n}{\pi}(x-t)\right) \right\} ,$$

where $\sum B_n \sin \frac{n}{\pi}x$ is the Fourier series of the $2L$ periodic odd extension of $g(x)$.